

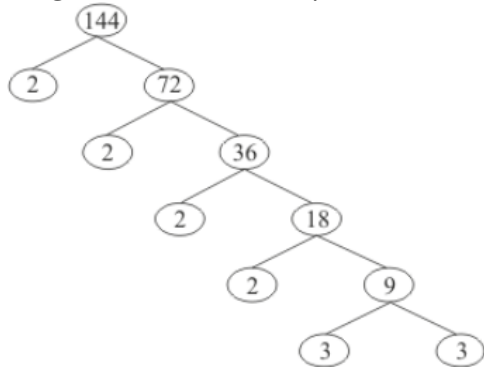
**Solution**  
**PRELIMINARY EXAM - I - SET B**  
**Class 10 - Mathematics**  
**Section A**

1.

**(d) 4**

**Explanation:**

Using the factor tree for prime factorisation, we have:



Therefore,  $144 = 2 \times 2 \times 2 \times 2 \times 3 \times 3$

$$\Rightarrow 144 = 2^4 \times 3^2$$

Thus, the exponent of 2 in 144 is 4.

2.

**(b) 0**

**Explanation:**

Here  $y = f(x)$  is not intersecting or touching the X-axis.

$\therefore$  Number of zeroes of  $f(x) = 0$

3.

**(c) 1**

**Explanation:**

The number of solutions of two linear equations representing intersecting lines is 1 because two linear equations representing intersecting lines has a unique solution.

4.

**(b)  $\frac{b^2}{4a}$**

**Explanation:**

If the quadratic equation  $ax^2 + bx + c = 0$  has two real and equal roots, then

$$b^2 - 4ac = 0$$

$$\Rightarrow b^2 = 4ac$$

$$\Rightarrow c = \frac{b^2}{4a}$$

5. **(a) 28**

**Explanation:**

$$a + 6d = 4 \Rightarrow a + 6 \times (-4) = 4 \Rightarrow a = 28$$

6. **(a) 5 units**

**Explanation:**

$X(-3, 0)$ ,  $O(0, 0)$ ,  $Y(0, 4)$ ,  $Z(x, y)$ .

XOYZ is a rectangle,

So, diagonal  $xy =$  diagonal  $OZ$

$$\begin{aligned}
 xy &= \sqrt{(-3-0)^2 + (0-4)^2} \\
 &= \sqrt{9+16} \\
 &= \sqrt{25} \\
 xy &= 5 \text{ units}
 \end{aligned}$$

7.

**(b)** (0, -10) and (4, 0)

**Explanation:**

Let the coordinates of P (0, y) and Q (x, 0).

So, the mid - point of P (0, y) and Q (x, 0) = M

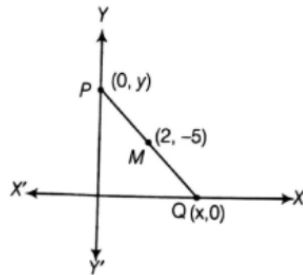
$$\text{Coordinates of } M = \left( \frac{0+x}{2}, \frac{y+0}{2} \right)$$

$\therefore$  Mid - point of a line segment having points  $(x_1, y_1)$  and  $(x_2, y_2)$

$$= \left( \frac{(x_1+x_2)}{2}, \frac{(y_1+y_2)}{2} \right)$$

Given,

Mid - point of PQ is (2, -5)



$$\therefore 2 = \frac{x+0}{2} = 4 = x + 0$$

$$x = 4$$

$$-5 = \frac{y+0}{2} = -10 = y + 0$$

$$-10 = y$$

So,

$$x = 4 \text{ and } y = -10$$

Thus, the coordinates of P and Q are (0, -10) and (4, 0)

8.

$$\text{(d) } DC^2 = CF \times AC$$

**Explanation:**

In  $\triangle ABC$ , using Thales theorem,

$$\frac{DC}{AC} = \frac{CE}{BC} \quad [AB \parallel DE] \dots\dots(i)$$

And in triangle BCD, using Thales theorem,

$$\frac{CF}{DC} = \frac{CE}{BC} \quad [BD \parallel EF] \dots\dots(ii)$$

From eq. (i) and (ii), we have

$$\frac{DC}{AC} = \frac{CF}{DC}$$

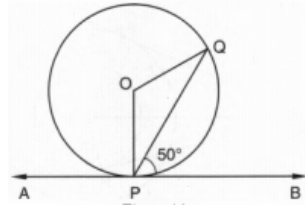
$$\Rightarrow DC^2 = CF \times AC$$

9.

**(d)**  $100^\circ$

**Explanation:**

In the figure, APB is a tangent to the circle with centre O



$$\angle OPB = 50^\circ$$

OP is radius and APB is a tangent

$$OP \perp AB$$

$$\Rightarrow \angle OPB = 90^\circ$$

$$\Rightarrow \angle OPQ + \angle QPB = 90^\circ$$

$$\angle OPQ + 50^\circ = 90^\circ$$

$$\Rightarrow \angle OPQ = 90^\circ - 50^\circ = 40^\circ$$

But  $OP = OQ$   $\angle OPQ = \angle OQP = 40^\circ$

$$\angle POQ = 180^\circ - (40^\circ + 40^\circ) = 180^\circ - 80^\circ = 100^\circ$$

10.

(c) 30 cm

**Explanation:**

$$AQ = AR = 4$$

Similarly,

$$PC = CQ = 5$$

Similarly,

$$BP = BR = 6$$

$$\text{Perimeter} = AB + BC + CA$$

$$\text{Perimeter} = AR + RB + BP + PC + CQ + QA$$

$$= 4 + 6 + 6 + 5 + 5 + 4$$

$$= 30 \text{ cm}$$

11. (a)  $\frac{1 - \cos \theta}{\sin \theta}$

**Explanation:**

$$\begin{aligned} \text{We have, } \frac{\sin \theta}{1 + \cos \theta} &= \frac{\sin \theta (1 - \cos \theta)}{(1 + \cos \theta)(1 - \cos \theta)} \\ &= \frac{\sin \theta (1 - \cos \theta)}{1 - \cos^2 \theta} = \frac{\sin \theta (1 - \cos \theta)}{\sin^2 \theta} \\ &= \frac{1 - \cos \theta}{\sin \theta} \end{aligned}$$

12. (a)  $\operatorname{cosec} \alpha$

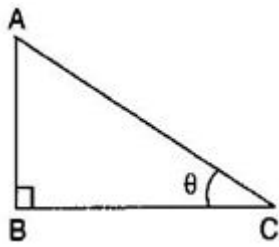
**Explanation:**

$$\begin{aligned} &1 + \frac{\cot^2 \alpha}{1 + \operatorname{cosec} \alpha} \\ &= 1 + \frac{\operatorname{cosec}^2 \alpha - 1}{1 + \operatorname{cosec} \alpha} \\ &= 1 + \frac{(\operatorname{cosec} \alpha - 1)(\operatorname{cosec} \alpha + 1)}{1 + \operatorname{cosec} \alpha} \\ &= 1 + \operatorname{cosec} \alpha - 1 = \operatorname{cosec} \alpha \end{aligned}$$

13.

(c) remains unchanged

**Explanation:**



Let height of the tower be  $h$  meters and distance of the point of observation from its foot be  $x$  meters and angle of elevation be  $\theta$   $\therefore \tan \theta = \frac{h}{x}$  .....(i)

Now, new height =  $h + 10\%$  of  $h = h + \frac{10}{100}h = \frac{11h}{10}$  And new distance =  $x + 10\%$  of  $x = x + \frac{10}{100}x = \frac{11x}{10}$

$$\therefore \tan \theta = \frac{\frac{11h}{10}}{\frac{11x}{10}} = \frac{h}{x} \text{ .....(ii)}$$

From eq. (i) and (ii), it is clear that the angle of elevation is same i.e., angle of elevation remains unchanged.

14.

**(b)**  $308 \text{ cm}^2$

**Explanation:**

We know that the area  $A$  of a sector of a circle of radius  $r$  and central angle  $\theta$  (in degrees) is given by

$$A = \frac{\theta}{360} \times \pi r^2$$

Here,  $r = 28 \text{ cm}$  and  $\theta = 45$ .

$$\therefore A = \frac{45}{360} \times \pi \times (28)^2 = \frac{1}{8} \times \frac{22}{7} \times 28 \times 28 \text{ cm}^2 = 308 \text{ cm}^2$$

15.

**(c)**  $77 \text{ cm}^2$

**Explanation:**

For a minute hand, 60 minutes is equivalent to  $360^\circ$  and so 30 minutes will be  $180^\circ$ .

Area swept in 60 minutes is area of full circle.

So area swept in 30 minutes will be area of half circle.

$$\text{Thus, area swept} = \frac{1}{2} \times \left(\frac{22}{7}\right) \times 7^2 = 77 \text{ cm}^2$$

16.

**(d)**  $\frac{4}{9}$

**Explanation:**

Total numbers of digits from 1 to 9 ( $n$ ) = 9

Numbers which are even ( $m$ ) = 2, 4, 6, 8 = 4

$$\therefore \text{Probability} = \frac{m}{n} = \frac{4}{9}$$

17.

**(b)** 0.24

**Explanation:**

Given:  $P$  (It will rain on a particular day) = 0.76

$\therefore P$  (It will not rain on a particular day) =  $1 - P$  (It will rain particular day)

$$= 1 - 0.76 = 0.24$$

18.

**(b)** 67.5

**Explanation:**

$$\begin{aligned}
 \text{Mode} &= l + \left( \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right) \times h \\
 &= 60 + \frac{16-6}{2 \times 16 - 6 - 6} \times 15 \\
 &= 60 + \frac{10}{32-12} \times 15 \\
 &= 60 + \frac{10}{20} \times 15 \\
 &= 60 + 7.5 \\
 &= 67.5
 \end{aligned}$$

19.

**(d)** A is false but R is true.

**Explanation:**

A is false but R is true.

20. **(a)** Both A and R are true and R is the correct explanation of A.

**Explanation:**

Both A and R are true and R is the correct explanation of A.

### Section B

21. To Prove:  $5+3\sqrt{2}$  is irrational number

Proof: If possible let us assume  $5 + 3\sqrt{2}$  is a rational number.

$$\Rightarrow 5 + 3\sqrt{2} = \frac{p}{q} \text{ where } q \neq 0 \text{ and } p \text{ and } q \text{ are coprime integers.}$$

$$\Rightarrow 3\sqrt{2} = \frac{p}{q} - 5$$

$$\Rightarrow 3\sqrt{2} = \frac{p-5q}{q}$$

$$\Rightarrow \sqrt{2} = \frac{p-5q}{3q}$$

$$\Rightarrow \sqrt{2} = \frac{\text{integer}}{\text{integer}}$$

$\Rightarrow \sqrt{2}$  is a rational number.

This contradicts the given fact that  $\sqrt{2}$  is irrational.

Hence  $5 + 3\sqrt{2}$  is an irrational number.

OR

Let us assume that  $7 - 2\sqrt{3}$  is a rational number

$$\Rightarrow 7 - 2\sqrt{3} = \frac{a}{b}, \text{ where } a \text{ and } b \text{ are integers, } b \neq 0$$

$$\Rightarrow \sqrt{3} = \frac{7b-a}{2b}$$

RHS is a rational number but LHS is irrational.

$\therefore$  Our assumption was wrong. Hence,  $7 - 2\sqrt{3}$  is irrational.

22. It is given that, AB = 5 cm, AC = 10 cm, BD = 1.5 cm and CD = 3.5 cm

We have to check whether AD is bisector of  $\angle A$

First we will check proportional ratio between sides

So,

$$\frac{AB}{AC} = \frac{5}{10} = \frac{1}{2}$$

$$\frac{BD}{CD} = \frac{1.5}{3.5} = \frac{3}{7}$$

$$\text{Since } \frac{AB}{AC} \neq \frac{BD}{CD}$$

Hence, AD is not the bisector of  $\angle A$

23. Let O be the centre of the given circle.

AB is the tangent drawn touching the circle at A.

Draw  $AC \perp AB$  at point A, such that point C lies on the given circle.

$\angle OAB = 90^\circ$  (Radius of the circle is perpendicular to the tangent)

Given  $\angle CAB = 90^\circ$

$\therefore \angle OAB = \angle CAB$

This is possible only when centre O lies on the line AC.

Hence, perpendicular at the point of contact to the tangent to a circle passes through the centre of the circle.

$$\begin{aligned}
 24. \text{ LHS} &= \frac{\tan^2 A}{1+\tan^2 A} + \frac{\cot^2 A}{1+\cot^2 A} \\
 &= \frac{\tan^2 A}{\sec^2 A} + \frac{\cot^2 A}{1+\cot^2 A} \\
 &= \frac{\frac{\sin^2 A}{\cos^2 A}}{\frac{1}{\cos^2 A}} + \frac{\frac{\cos^2 A}{\sin^2 A}}{\frac{1}{\sin^2 A}} \\
 &= \frac{\sin^2 A}{\cos^2 A} \times \frac{\cos^2 A}{1} + \frac{\cos^2 A}{\sin^2 A} \times \frac{\sin^2 A}{1} \\
 &= \sin^2 A + \cos^2 A \\
 &= 1 \quad [\because \sin^2 A + \cos^2 A = 1] \\
 &= \text{RHS} \\
 &\text{Hence proved.}
 \end{aligned}$$

OR

$$\begin{aligned}
 \frac{1}{1-\sin \theta} + \frac{1}{1+\sin \theta} &= 2 \sec^2 \theta \\
 \text{L.H.S.} &= \frac{1}{1-\sin \theta} + \frac{1}{1+\sin \theta} \\
 &= \frac{1+\sin \theta + 1-\sin \theta}{(1-\sin \theta)(1+\sin \theta)} = \frac{2}{1-\sin^2 \theta} \\
 &= \frac{2}{\cos^2 \theta} \quad [\because 1 - \sin^2 \theta = \cos^2 \theta] \\
 &= 2 \sec^2 \theta \quad [\because \sec(x) = \frac{1}{\cos(x)}] \\
 &= \text{R.H.S. Proved}
 \end{aligned}$$

25. i. Area of sector OAPB =  $\frac{90^\circ}{360^\circ} \times 3.14 \times 100 = 78.5 \text{ cm}^2$   
 ii. Area minor segment APB = Area sector OAPB - Area  $\triangle OAB$   
 $= 78.5 - \frac{1}{2} \times 100$   
 $= 28.5 \text{ cm}^2.$

### Section C

26. The required greatest capacity is the HCF of 120, 180 and 240.

$$240 = 180 \times 1 + 60$$

$$180 = 60 \times 3 + 0$$

HCF is 60.

Now HCF of 60, 120

$$120 = 60 \times 2 + 0$$

$\therefore$  HCF of 120, 180 and 240 is 60.

$\therefore$  The required capacity is 60 litres.

27. Let  $P(x) = 2x^2 + 3x + \lambda$

Its one zero is  $\frac{1}{2}$  so  $P(\frac{1}{2}) = 0$

$$P(\frac{1}{2}) = 2 \times (\frac{1}{2})^2 + 3(\frac{1}{2}) + \lambda = 0$$

$$\Rightarrow 2 \times \frac{1}{4} + \frac{3}{2} + \lambda = 0$$

$$\Rightarrow \frac{1}{2} + \frac{3}{2} + \lambda = 0$$

$$\Rightarrow \frac{4}{2} + \lambda = 0$$

$$\Rightarrow 2 + \lambda = 0$$

$$\Rightarrow \lambda = -2$$

Let the other zero be  $\alpha$

$$\text{Then } \alpha + \frac{1}{2} = -\frac{3}{2}$$

$$\Rightarrow \alpha = -\frac{3}{2} - \frac{1}{2} = -\frac{4}{2} = -2$$

28. First, we will convert the graph given into tabular form as shown below:

Class interval	Frequency (f <sub>i</sub> )	Mid value (x <sub>i</sub> )	f <sub>i</sub> x <sub>i</sub>	Cumulative Frequency
1 - 4	6	2.5	15	6

4 - 7	30	5.5	165	36
7 - 10	40	8.5	340	76
10 - 13	16	11.5	184	92
13 - 16	4	14.5	58	96
16 - 19	4	17.5	70	100
	$N = \sum f_i = 100$		$\sum f_i x_i = 832$	

i.  $N = 100$

$$\text{Mean} = \frac{\sum f_i x_i}{N} = \frac{832}{100} = 8.32$$

ii.  $\frac{N}{2} = \frac{100}{2} = 50$

The cumulative frequency just greater than  $\frac{N}{2}$  is 76, then the median class is 7 - 10 such that  $l = 7, h = 10 - 7 = 3, f = 40, F = 36$

$$\begin{aligned} \text{Median} &= l + \frac{\frac{N}{2} - F}{f} \times h \\ &= 7 + \frac{50 - 36}{40} \times 3 \\ &= 7 + \frac{42}{40} = 7 + 1.05 = 8.05 \end{aligned}$$

iii. Mode = 3 Median - 2 Mean

$$= 3 \times 8.05 - 2 \times 8.32 = 7.51$$

29. Let the amount invested at 12% be ₹x and that invested at 10% be ₹y.

Then, total annual interest

$$= \left( \frac{x \times 12 \times 1}{100} + \frac{y \times 10 \times 1}{100} \right) = \left( \frac{6x + 5y}{50} \right)$$

$$\therefore \frac{6x + 5y}{50} = 2600 \Rightarrow 6x + 5y = 130000 \dots\dots(i)$$

Again, the amount invested at 12% is ₹y and that invested at 10% is ₹x.

Total annual interest at the new rates

$$= \left( \frac{y \times 12 \times 1}{100} + \frac{x \times 10 \times 1}{100} \right) = \left( \frac{6y + 5x}{50} \right)$$

But, interest received at the new rates = ₹(2600 - 140) = ₹2460.

$$\therefore \frac{6y + 5x}{50} = 2460 \Rightarrow 5x + 6y = 123000 \dots\dots(ii)$$

Adding (i) and (ii), we get

$$11x + 11y = 253000$$

$$\Rightarrow 11(x + y) = 253000 \Rightarrow x + y = 23000 \dots (iii)$$

Subtracting (ii) from (i), we get

$$x - y = 7000 \dots(iv)$$

Adding (iii) and (iv), we get  $2x = 30000 \Rightarrow x = 15000$ .

Putting  $x = 15000$  in (i), we get

$$15000 + y = 23000 \Rightarrow y = 23000 - 15000 = 8000$$

$\therefore x = 15000$  and  $y = 8000$ .

Hence, the amount at 12% is ₹15000 and that at 10% is ₹8000.

OR

Let fixed charge be Rs x and charge taken per day for food be Rs y

$$x + 20y = 3000 \dots\dots(i)$$

$$x + 25y = 3500 \dots\dots(ii)$$

Subtracting (i) from (ii)

$$\begin{array}{r} x + 25y = 3500 \\ x + 20y = 3000 \\ \hline 5y = 500 \\ y = 100 \end{array}$$

Substituting this value of y in (i)

$$x + 20(100) = 3000$$

$$x = 1000$$

$$x = 1000 \text{ and } y = 100$$

Fixed charge and cost of food per day are Rs 1000 and Rs100

$$30. = (m + n)^{2/3} + (m - n)^{2/3}$$

$$= (a\cos^3\theta + 3a\cos\theta\sin^2\theta + a\sin^2\theta + 3a\cos^2\theta\sin\theta)^{2/3} + (a\cos^3\theta + 3a\cos\theta\sin^2\theta - a\sin^3\theta - 3a\cos^2\theta\sin\theta)^{2/3}$$

$$= a^{2/3}(\cos^3\theta + 3\cos\theta\sin^2\theta + \sin^3\theta + 3\cos^2\theta\sin\theta)^{2/3} + a^{2/3}(\cos^3\theta + 3\cos\theta\sin^2\theta - \sin^3\theta - 3\cos^2\theta\sin\theta)^{2/3}$$

$$= a^{2/3}\{(\cos\theta + \sin\theta)^3\}^{2/3} + a^{2/3}\{(\cos\theta - \sin\theta)^3\}^{2/3}$$

$$= a^{2/3}(\cos\theta + \sin\theta)^2 + a^{2/3}(\cos\theta - \sin\theta)^2$$

$$= a^{2/3}(\cos^2\theta + \sin^2\theta + 2\cos\theta\sin\theta) + a^{2/3}(\cos^2\theta + \sin^2\theta - 2\cos\theta\sin\theta)$$

$$= a^{2/3}(1 + 2\cos\theta\sin\theta) + a^{2/3}(1 - 2\cos\theta\sin\theta) \quad [\because \cos^2\theta + \sin^2\theta = 1]$$

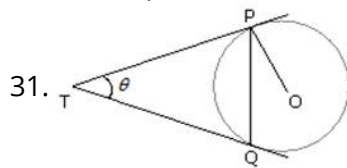
$$= a^{2/3}(1 + 2\cos\theta\sin\theta + 1 - 2\cos\theta\sin\theta)$$

$$= a^{2/3}(1 + 1)$$

$$= 2a^{2/3}$$

$$= \text{RHS}$$

Hence proved.



Given A circle with centre O and an external point T and two tangents TP and TQ to the circle, where P, Q are the points of contact.

To Prove:  $\angle PTQ = 2\angle OPQ$

Proof: Let  $\angle PTQ = \theta$

Since TP, TQ are tangents drawn from point T to the circle.

$$TP = TQ$$

$\therefore$  TPQ is an isoscles triangle

$$\therefore \angle TPQ = \angle TQP = \frac{1}{2} (180^\circ - \theta) = 90^\circ - \frac{\theta}{2}$$

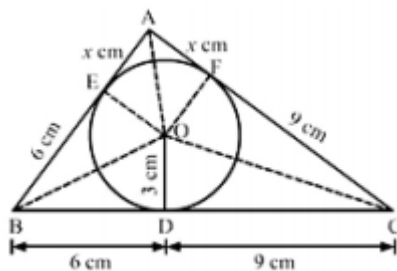
Since, TP is a tangent to the circle at point of contact P

$$\therefore \angle OPT = 90^\circ$$

$$\therefore \angle OPQ = \angle OPT - \angle TPQ = 90^\circ - (90^\circ - \frac{1}{2} \theta) = \frac{\theta}{2} = \frac{1}{2} \angle PTQ$$

Thus,  $\angle PTQ = 2\angle OPQ$

OR



We know that tangent segments to a circle from the same external point are congruent

Now, we have

$$AE = AF,$$

$$BD = BE = 6 \text{ cm and}$$

$$CD = CF = 9 \text{ cm}$$

Now,

$$\text{Area}(\triangle ABC)$$

$$= \text{Area}(\triangle BOC) + \text{Area}(\triangle AOB) + \text{Area}(\triangle AOC)$$

$$\Rightarrow 54 = \frac{1}{2} \times BC \times OD + \frac{1}{2} \times AB \times OE + \frac{1}{2} \times AC \times OF$$

$$\Rightarrow 108 = 15 \times 3 + (6 + x) \times 3 + (9 + x) \times 3$$



$$\begin{aligned}\Rightarrow 36 &= 15 + 6 + x + 9 + x \\ \Rightarrow 36 &= 30 + 2x \\ \Rightarrow 2x &= 6 \\ \Rightarrow x &= 3\text{cm} \\ \therefore AB &= 6 + 3 = 9\text{cm and} \\ AC &= 9 + 3 = 12\text{cm.}\end{aligned}$$

### Section D

32. From the given table

Monthly Consumption	Number of Families (f)	Cumulative frequency (C.f.)
130 - 140	5	5
140 - 150	9	14
150 - 160	17	31
160 - 170	28	59
170 - 180	24	83
180 - 190	10	93
190 - 200	7	100

We have,  $N = 100$

$$\frac{N}{2} = 50$$

Median class = 160 - 170

$$\Rightarrow l = 160, f = 28, Cf = 31, h = 10$$

$$\text{Median} = l + \left[ \frac{\left(\frac{N}{2} - Cf\right)}{f} \right] \times h$$

$$= 160 + \left[ \frac{(50 - 31)}{28} \right] \times 10$$

$$= 160 + \left[ \frac{19}{28} \right] \times 10$$

$$= 160 + 6.78$$

$$= 166.78$$

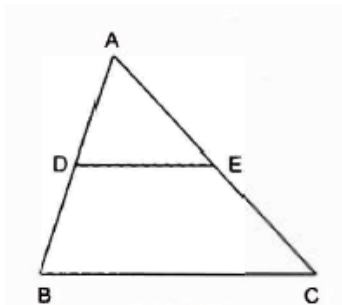
33. We have,

Area ( $\triangle ADE$ ) = Area (trapezium BCED)

$$\Rightarrow \text{Area} (\triangle ADE) + \text{Area} (\triangle ADE) = \text{Area} (\text{trapezium BCED}) + \text{Area} (\triangle ADE)$$

$$\Rightarrow 2 \text{Area} (\triangle ADE) = \text{Area} (\triangle ABC) \dots(i)$$

In  $\triangle ADE$  and  $\triangle ABC$ , we have



$DE \parallel BC$ , therefore,  $\angle ADE = \angle B$  [Corresponding angles]

and,  $\angle A = \angle A$  [Common]

$$\therefore \triangle ADE \sim \triangle ABC$$

Since for similar triangles, the ratio of the areas is the square of the ratio of their corresponding sides. Therefore,

$$\frac{\text{Area} (\triangle ADE)}{\text{Area} (\triangle ABC)} = \frac{AD^2}{AB^2}$$

$$\Rightarrow \frac{\text{Area}(\triangle ADE)}{2 \text{Area}(\triangle ADE)} = \frac{AD^2}{AB^2}$$

$$\Rightarrow \frac{1}{2} = \left(\frac{AD}{AB}\right)^2$$

$$\Rightarrow \frac{AD}{AB} = \frac{1}{\sqrt{2}}$$

$$\Rightarrow AB = \sqrt{2}AD$$

$$\Rightarrow AB = \sqrt{2}(AB - BD)$$

$$\Rightarrow (\sqrt{2} - 1)AB = \sqrt{2}BD \Rightarrow \frac{BD}{AB} = \frac{\sqrt{2}-1}{\sqrt{2}} = \frac{2-\sqrt{2}}{2}$$

34. Since (-5) is a root of given quadratic equation  $2x^2 + px + 15 = 0$ , then,

$$2(-5)^2 + p(-5) - 15 = 0$$

$$50 - 5p - 15 = 0$$

$$5p = 35 \Rightarrow p = 7$$

Now  $p(x^2 + x) + k = 0$  has equal roots

$$px^2 + px + k = 0$$

$$\text{So } (b)^2 - 4ac = 0$$

$$(p)^2 - 4p \times k = 0$$

$$(7)^2 - 4 \times 7 \times k = 0$$

$$28k = 49$$

$$k = \frac{49}{28} = \frac{7}{4}$$

$$\text{hence } p = 7 \text{ and } k = \frac{7}{4}$$

OR

Distance travelled by the train = 480 km

Let the speed of the train be  $x$  kmph

$$\text{Time taken for the journey} = \frac{480}{x}$$

Given speed is decreased by 8 kmph

Hence the new speed of train =  $(x - 8)$  kmph

$$\text{Time taken for the journey} = \frac{480}{x-8}$$

$$\frac{480}{x-8} = \frac{480}{x} + 3$$

$$\Rightarrow \frac{480}{x-8} - \frac{480}{x} = 3$$

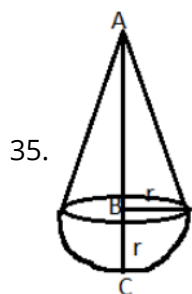
$$\Rightarrow \frac{480(x-x+8)}{x(x-8)} = 3$$

$$\Rightarrow \frac{480 \times 8}{x(x-8)} = 3$$

$$\Rightarrow 3x(x-8) = 480 \times 8$$

$$\Rightarrow x(x-8) = 160 \times 8$$

$$\Rightarrow x^2 - 8x - 1280 = 0$$



From the given figure,

Height (AB) of the cone = AC - BC (Radius of the hemisphere)

Thus, height of the cone = Total height - Radius of the hemisphere

$$= 9.5 - 3.5$$

$$= 6 \text{ cm}$$

Volume of the solid = Volume of the cone + Volume of the hemisphere

$$\begin{aligned}
&= \left(\frac{1}{3}\pi r^2 h\right) + \left(\frac{2}{3}\pi r^3\right) \\
&= \frac{1}{3}\pi r^2(h + 2r) \\
&= \frac{1}{3} \times \frac{22}{7} \times 3.5 \times 3.5(6 + 2 \times 3.5) \\
&= \frac{1}{3} \times \frac{22}{7} \times 3.5 \times 3.5 \times 13 \\
&= 166.83 \text{ cm}^3
\end{aligned}$$

Thus, total volume of the solid is  $166.83 \text{ cm}^3$ .

OR

Given side of a cube = 21 cm

Diameter of the hemisphere is equal to the side of the cubical piece (d) = 21 cm

$\Rightarrow$  Radius of the hemisphere = 10.5 cm

Volume of cube = Side<sup>3</sup>

$$= (21)^3$$

$$= 9261 \text{ cm}^3$$

Surface area of cubical piece of wood =  $6a^2$

$$= 6 \times 21 \times 21 \text{ cm}^2$$

$$= 2646 \text{ cm}^2$$

Volume of the hemisphere =  $\frac{2}{3}\pi r^3$

$$= \frac{2}{3} \times \frac{22}{7} \times 10.5 \times 10.5 \times 10.5$$

$$= 44 \times 0.5 \times 10.5 \times 10.5$$

$$= 2425.5 \text{ cm}^3$$

Surface area of hemisphere =  $2\pi r^2$

$$= 2 \times \pi \times 10.5 \times 10.5 \text{ cm}$$

$$= 693 \text{ cm}^2$$

Volume of remaining solid = Volume of cubical piece of wood – Volume of hemisphere

$\Rightarrow$  Volume of the remaining solid =  $9261 - 2425.5$

$$= 6835.5 \text{ cm}^3$$

Surface area remaining piece of solid = surface area of cubical piece of wood – Area of circular base of hemisphere + Curved Surface area of hemisphere

$$= 6a^2 - \pi r^2 + 2\pi r^2$$

$$= (2646 - \pi \times 10.5^2 + 693) \text{ cm}^2$$

$$= 2992.5 \text{ cm}^2.$$

### Section E

36. i. Let production in a 1st year be 'a' unit and increase in production (every year) be 'd' units.

Increase in production is constant, therefore unit produced every year forms an AP.

Now,  $a_3 = 6000$

$$a + 2d = 6000 \Rightarrow a = 6000 - 2d \dots(i)$$

$$\text{and } a_7 = 7000 \Rightarrow a + 6d = 7000$$

$$\Rightarrow (6000 - 2d) + 6d = 7000 \Rightarrow 4d = 1000 \text{ [using eq. (i)]}$$

$$\Rightarrow d = 250$$

When  $d = 250$ , eq. (i) becomes

$$a = 6000 - 2(250) = 5500$$

$\therefore$  Production in 1st year = 5500

- ii. Production in fifth year

$$a_5 = a + 4d = 5500 + 4(250) = 6500$$

- iii. Total production in 7 years =  $\frac{7}{2}(5500 + 7000) = 43750$

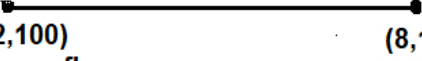
OR

$$a_n = 1000 \text{ units}$$

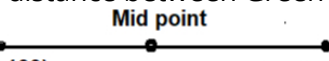
$$a_n = 1000$$

$$\begin{aligned}\Rightarrow 10000 &= a + (n - 1)d \\ \Rightarrow 1000 &= 5500 + 250n - 250 \\ \Rightarrow 10000 - 5500 + 250 &= 250n \\ \Rightarrow 4750 &= 250n \\ \Rightarrow n &= \frac{4750}{250} = 19\end{aligned}$$

37. i. Co-ordinate of green flag = (2,100)

ii.   
**Green flag** **Red flag**  
 distance between Red flag and Green flag  
 $d = \sqrt{(8 - 2)^2 + (100 - 100)^2}$   
 $= \sqrt{6^2 + 0^2}$   
 $d = 6$

$\therefore$  distance between Green and Red flag is 6 m.

iii.   
**Green flag** **Red flag**  
 Position of blue flag =  $\left( \frac{2+8}{2}, \frac{100+100}{2} \right)$   
 $= (5, 100)$

**OR**

$$\begin{aligned}\text{Distance} &= \sqrt{(5 - 2)^2 + (100 - 100)^2} \\ &= \sqrt{9 + 0} \\ &= 3 \text{ m}\end{aligned}$$

38. i. In  $\triangle ABC$

$$\tan 60^\circ = \frac{AB}{BC}$$

$$\sqrt{3} = \frac{AB}{200}$$

$$AB = 200\sqrt{3}$$

Now, In  $\triangle ABD$

$$\tan 45^\circ = \frac{AB}{BD}$$

$$1 = \frac{200\sqrt{3}}{BD}$$

$$BD = 200\sqrt{3}$$

$$\therefore CD = BD - BC$$

$$= 200\sqrt{3} - 200$$

$$= 200(\sqrt{3} - 1)$$

$$= 200 \times (1.732 - 1)$$

$$= 200 \times 0.732$$

$$= 146.4 \text{ m}$$

$$\text{speed} = \frac{\text{distance}}{\text{time}}$$

$$= \frac{146.4}{10}$$

$$= 14.64 \text{ m/s}$$

Now,

$$\text{speed} = 14.64 \times \frac{18}{5} \text{ km/hr}$$

$$= 52.7$$

$$\approx 53 \text{ km/hr}$$

ii. In  $\triangle ABD$

$$\tan 45^\circ = \frac{AB}{BD}$$

$$1 = \frac{200\sqrt{3}}{BD}$$

$$BD = 200\sqrt{3} \text{ m}$$

$$\therefore CD = 200\sqrt{3} - 200$$

$$\begin{aligned}
 &= 200 (\sqrt{3} - 1) \\
 &= 200 (1.732 - 1) \\
 &= 200 \times 0.732 \\
 &= 146.4 \\
 &\approx 147 \text{ m}
 \end{aligned}$$

$\therefore$  boat is at a distance of 147 m from its actual position.

iii. In  $\triangle ABC$

$$\tan 60^\circ = \frac{AB}{BC}$$

$$\sqrt{3} = \frac{AB}{200}$$

$$AB = 200\sqrt{3} \text{ m}$$

$$\text{Hence, height of tower} = 200\sqrt{3} \text{ m}$$

**OR**

As boat moves away from the tower angle of depression decreases.