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2025 XII 30 1100 – N 926 – MATHEMATICS (71) GEOMETRY- PART II (E)

**(NEW COURSE)**

Time : 2 Hours

(Pages 6)

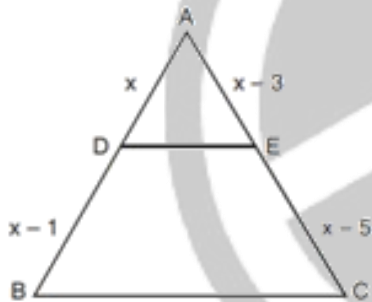
Max. Marks : 40

- Note :-** (i) All questions are compulsory.  
(ii) Use of calculator is not allowed.  
(iii) Total marks are shown on the right side of the question.

**Q.1(A) Choose the correct alternative:**

**4**

- (1) In  $\Delta PQR$ , seg  $PM$  is a median.  $PM = 7$  and  $PQ^2 + PR^2 = 340$ . Find  $QR$ .  
(a) 16 units (b) 22 units (c) 11 units (d) 32 units
- (2) If a tangent has to be drawn to a circle without using centre, a \_\_\_\_\_ is drawn in a circle.  
(a) circle (b) tangent (c) rectangle (d) triangle
- (3) In  $\Delta ABC$ ,  $DE \parallel BC$ . In the figure the value of  $x$  is \_\_\_\_\_.

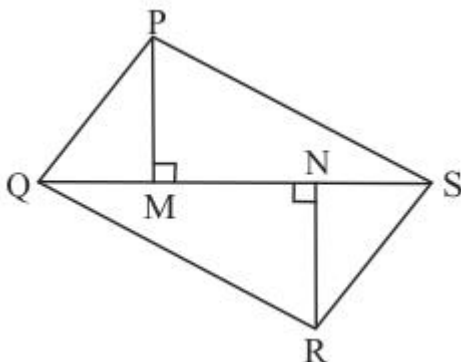


- (a) 1 (b) 3 (c) -1 (d) -3
- (4) The ratio of circumference and area of a circle is 2:7. Find its circumference.  
(A)  $14\pi$  (B)  $\frac{7}{\pi}$  (C)  $7\pi$  (D)  $\frac{14}{\pi}$

**(B) Solve the following:**

**4**

- (1) In figure below,  $PM = 10$  cm  $A(\Delta PQS) = 100$  sq. cm  $A(\Delta QRS) = 110$  sq. cm then find  $NR$ .



- (2) The ratio of corresponding sides of similar triangles is 3 : 5, then find the ratio of their areas.

(3) Find the Y –co-ordinate of the centroid of a triangle whose vertices are (4, -3), (7, 5) and (-2, 1).

(4) Prove the following:  $\tan^4 \theta + \tan^2 \theta = \sec^4 \theta - \sec^2 \theta$

**Q.2(A) Complete the following activities:(Any TWO)**

**4**

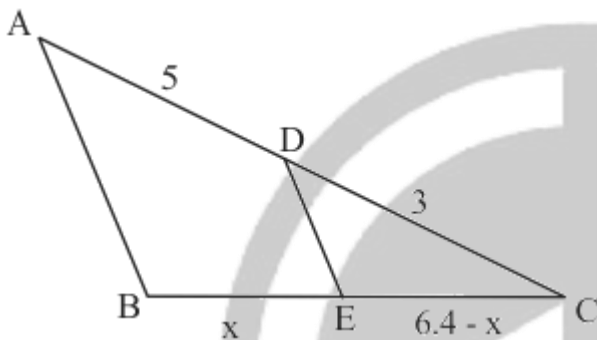
(1) Complete the following activity to prove:  $\cot \theta + \tan \theta = \operatorname{cosec} \theta \times \sec \theta$

$$\text{L.H.S.} = \cot \theta + \tan \theta$$

$$\begin{aligned} &= \frac{\cos \theta}{\sin \theta} + \frac{\boxed{\phantom{000}}}{\cos \theta} = \frac{\boxed{\phantom{000}} + \sin^2 \theta}{\sin \theta \times \cos \theta} \\ &= \frac{1}{\sin \theta \times \cos \theta} \dots \therefore \boxed{\phantom{000}} = \frac{1}{\sin \theta} \times \frac{1}{\cos \theta} \\ &= \boxed{\phantom{000}} \times \sec \theta \end{aligned}$$

$$\therefore \text{L.H.S.} = \text{R.H.S.}$$

(2) In figure below A – D – C and B – E – C seg DE  $\parallel$  side AB If AD = 5, DC = 3, BC = 6.4 then find BE.



Let BE = x units [supposition]

BC = BE + CE [B – E – C]

$$\therefore 6.4 = x + CE$$

$$\therefore CE = (6.4 - x) \text{ units}$$

In  $\triangle ABC$ , seg DE  $\parallel$  side AB [Given]

$$\therefore \frac{AD}{DC} = \frac{BE}{EC}$$

$$\therefore \frac{5}{3} = \frac{x}{\boxed{\phantom{000}}}$$

$$\therefore 5(6.4 - x) = 3x$$

$$\therefore \boxed{\phantom{000}} \times 5 - 5x = 3x$$

$$\therefore 6.4 \times 5 = 3x + \boxed{\phantom{000}}$$

$$\therefore \frac{6.4 \times 5}{8} = x$$

$$\therefore x = \boxed{\phantom{000}}$$

$$\therefore BE = 4 \text{ units}$$

(3) How many solid cylinders of radius 6 cm and height 12 cm can be made by melting a solid sphere of radius 18 cm ?

Activity: Radius of the sphere,  $r = 18$  cm  
 For cylinder, radius  $R = 6$  cm, height  $H = 12$

$$\therefore \text{Number of cylinders can be made} = \frac{\text{Volume of the sphere}}{\boxed{\phantom{0000}}}$$

$$= \frac{\frac{4}{3}\pi r^3}{\boxed{\phantom{0000}}}$$

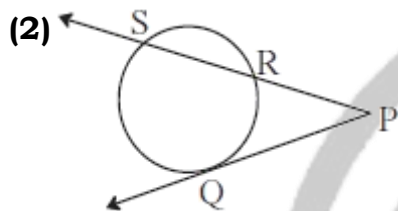
$$= \frac{\frac{4}{3} \times 18 \times 18 \times 18}{\boxed{\phantom{0000}}}$$

$$= \boxed{\phantom{0000}}$$

**(B) Solve the following: (Any FOUR)**

**8**

**(1)** Draw a circle of radius 3.6 cm. Draw a tangent to the circle at any point on it without using the centre.

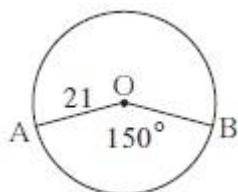


In the figure Q is the contact point. If  
 $PQ = 12$ ,  $PR = 8$ , then  $PS = ?$

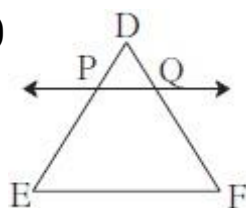
**(3)** In trapezium ABCD, side  $AB \parallel$  side  $PQ \parallel$  side  $DC$ ,  $AP = 15$ ,  $PD = 14$ ,  $QC = 14$ , find BQ.



**(4)** The measure of a central angle of a circle is  $150^\circ$  and radius of the circle is 21 cm. Find the length of the arc and area of the sector associated with the central angle.



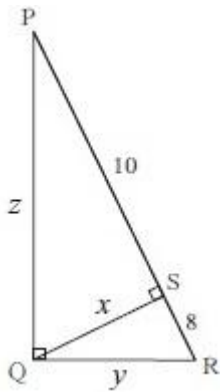
**(5)**



In  $\triangle DEF$ , line  $PQ \parallel$  side  $EF$ , If  $DP = 2.4$ ,  
 $PE = 7.2$ ,  $PQ = 1$  then find QF.

**Q.3(A) Complete the following activity:(Any ONE)****3**

- (1) In the figure below .In  $\Delta PQR$ ,  $\angle PQR = 90^\circ$ , seg  $QS \perp$  seg  $PR$  then find  $x$ ,  $y$ ,  $z$ .



In  $\Delta PQR$ ,  $\angle PQR = 90^\circ$ , seg  $QS \perp$  seg  $PR$

$$QS = \sqrt{PS \times SR} \dots\dots\dots (\text{theorem of geometric mean})$$

$$= \sqrt{10 \times 8}$$

$$= \sqrt{5 \times 2 \times 8}$$

$$= \sqrt{5 \times 16}$$

$$= \boxed{\phantom{00}}$$

In  $\Delta QSR$ , by Pythagoras theorem

$$QR^2 = QS^2 + SR^2$$

$$= (4\sqrt{5})^2 + 8^2$$

$$= 16 \times 5 + \boxed{\phantom{00}}$$

$$= 80 + 64$$

$$= \boxed{\phantom{00}}$$

$$\therefore QR = \boxed{\phantom{00}}$$

In  $\Delta PSQ$ , by Pythagoras theorem

$$PQ^2 = QS^2 + PS^2$$

$$= (4\sqrt{5})^2 + 10^2$$

$$= 16 \times 5 + 100$$

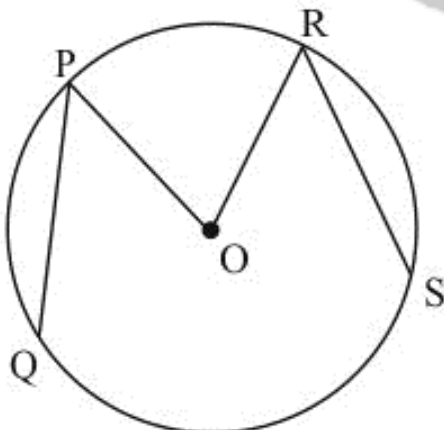
$$= 80 + 100$$

$$= \boxed{\phantom{00}}$$

$$= 36 \times 5$$

$$\therefore PQ = \boxed{\phantom{00}}$$

- (2) In figure below, O is the centre of a circle, chord  $PQ \cong$  chord  $RS$  If  $\angle POR = 70^\circ$  and  $(\text{arc } RS) = 80^\circ$ , find



- (1)  $m(\text{arc } PR)$
- (2)  $m(\text{arc } QS)$
- (3)  $m(\text{arc } QSR)$

$$M(\text{arc PR}) = m \angle POR$$

[Definition of measure of minor arc]

$$\therefore m(\text{arc PR}) = \boxed{\phantom{00}} \dots 1$$

$$\text{Chord PQ} \cong \text{chord } \boxed{\phantom{00}} \quad [\text{Given}]$$

$$\therefore \boxed{\phantom{00}} \cong (\text{arc RS})$$

[In a circle, congruent chords have corresponding minor arcs congruent]

$$\therefore m(\text{arc PQ}) = \boxed{\phantom{00}} \dots 2$$

$$M(\text{arc PR}) + m(\text{arc RS}) + m(\text{arc PQ}) + m(\text{arc QS}) = 360^\circ \quad [\text{Measure of a circle}]$$

$$\therefore 70^\circ + 80^\circ + 80^\circ + m(\boxed{\phantom{00}}) = 360^\circ$$

$$\therefore m(\text{arc QS}) = 360^\circ - 230^\circ$$

$$\therefore m(\text{arc QS}) = 130^\circ \dots 3$$

$$M(\text{arc QSR}) = m(\text{QS}) + m(\text{arc SR})$$

[Arc addition property]

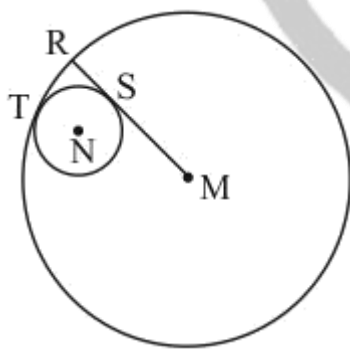
$$\therefore m(\text{arc QSR}) = 130^\circ + 80^\circ$$

$$\therefore m(\text{arc QSR}) = \boxed{\phantom{00}}$$

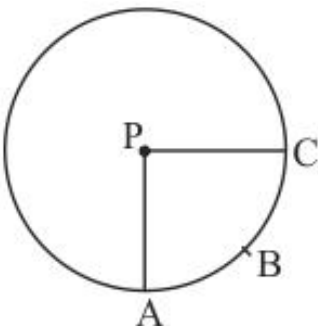
**(B) Solve the following: (Any TWO)**

**6**

- (1) The radius of a circle with centre P is 10 cm. If chord AB of the circle subtends a right angle at P, find areas of the minor segment and the major segment. ( $\pi = 3.14$ )
- (2) Find the ratio in which point P(k, 7) divides the segment joining A(8, 9) and B(1, 2). Also find k.
- (3) In figure below, circle with centre M touches the circle with centre N at point T. Radius RM touches the smaller circle at S. Radii of circles are 9 cm and 2.5 cm. Find the answers to the following questions hence find the ratio MS:SR.
  - (1) Find the length of segment MT
  - (2) Find the length of seg MN
  - (3) Find the measure of  $\angle NSM$ .

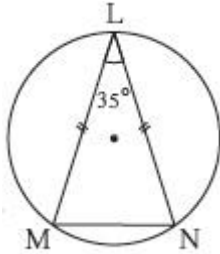


- (4) In the figure below, If  $A(P - ABC) = 154 \text{ cm}^2$  radius of the circle is 14 cm, find
  - (1)  $\angle APC$ .
  - (2)  $l(\text{arc ABC})$

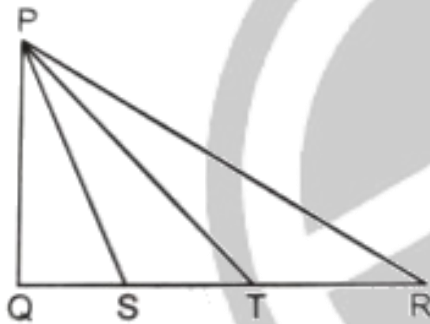


**Q.4 Solve the following: (Any TWO)****8**

- (1) Find the coordinates of the points which divide the line segment joining the points  $(-2, 2)$  and  $(6, -6)$  in four equal parts.
- (2) The area of the base of a cone is  $78.5 \text{ cm}^2$ . Its slant height is  $7 \text{ cm}$ . Find total surface area and height of the cone.
- (3) In figure below, chord  $LM \cong$  chord  $LN$   $\angle L = 35^\circ$  find  
(i)  $m(\text{arc } MN)$   
(ii)  $m(\text{arc } LN)$

**Q.5 Solve the following: (Any ONE)****3**

- (1) The angle of elevation of a jet plane from a point on the ground is  $60^\circ$ . After a flight of  $30 \text{ sec}$ , the angle of elevation changes to  $30^\circ$ . If the jet plane is flying at a constant height of  $3600\sqrt{3} \text{ m}$ , find the speed of the jet plane.
- (2) In the given figure,  $\Delta PQR$  is right angled at  $Q$  and the points  $S$  and  $T$  trisect the side  $QR$ . Prove that  $8PT^2 = 3PR^2 + 5PS^2$



**....All The Best....**



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**CIDCO BRANCH**

9168 444 999

1<sup>ST</sup> FLOOR, INFRONT OF BALIRAM PATIL SCHOOL

**HARSUL-SAWANGI BRANCH**

9168 044 999

1<sup>ST</sup> FLOOR, INFRONT OF PANAD SUPER MARKET